IIT-JEE 2009 Physics Paper - II

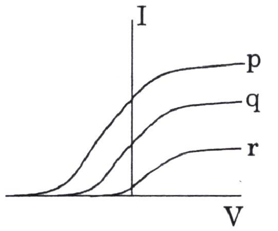
PART III - Physics

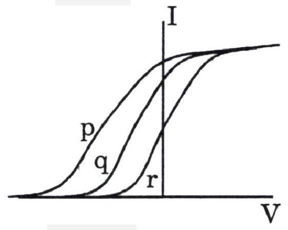
SECTION I - Straight Objective Type

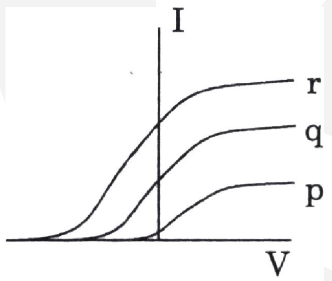
39. A piece of wire is bent in the shape of a parabola $y = kx^2$ (y-axis vertical) with a bead of mass m on it. The bead can slide on the wire without friction. It stays at the lowest point of the parabola when the wire is at rest. The wire is now accelerated parallel to the x-axis with a constant acceleration a. The distance of the new equilibrium position of the bead, where the bead can stay at rest with respect to the wire, from the y-axis is
(A) a / gk (B) $a / 2gk$ (C) $2a / gk$ (D) $a / 4gk$

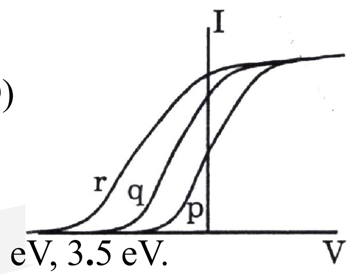
39. **(B)** $g \sin \theta = a \cos \theta \Rightarrow a / g = 1 \tan \theta = dy / dx = 2kx. \quad \Rightarrow |x| = a / 2gk$

40. Photoelectric effect experiments are performed using three different metal plates p, q and r having work functions $\phi_p = 2.0$ eV, $\phi_q = 2.5$ eV and $\phi_r = 3.0$ eV, respectively. A light beam containing wavelengths of 550 nm, 450 nm and 350 nm with equal intensities illuminates each of the plates. The correct I–V graph for the experiment is

(A)


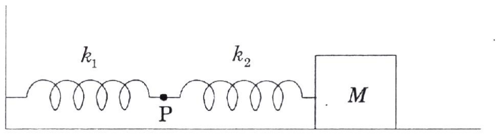
(B)


(C)


(D)


40. **(A)** Wavelength have energies 2.25 eV, 2.75 eV, 3.5 eV.
$\therefore$ In P, all cause emission, in q, only last two & in r, only last $\therefore I_P > I_q > I_r$.

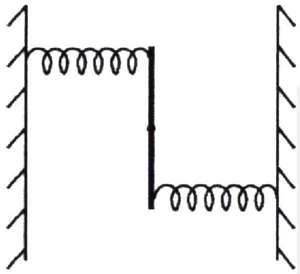
41. The mass M shown in the figure oscillates in simple harmonic motion with amplitude A. The amplitude of the point P is



(A) $k_2 A / k_2$ (B) $k_2 A / k_2$ (C) $k_1 A / k_1 + k_2$ (D) $k_2 A / k_1 + k_2$

41. **(D)** $K_1 A_P = K_2 (A - A_P) \Rightarrow A_P = K_2 A / (k_1 + k_2)$.

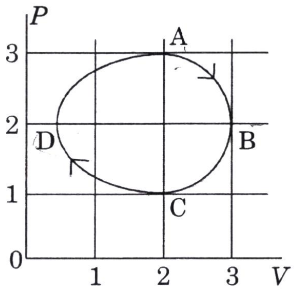
42. A uniform rod of length L and mass M is pivoted at the centre. Its two ends are attached to two springs of equal spring constants k. The springs are fixed to rigid supports as shown in the figure, and the rod is free to oscillate in the horizontal plane. The rod is gently pushed through a small angle θ in one direction and released. The frequency of oscillation is



(A) $1 / 2\pi\sqrt{2k / M}$ (B) $1 / 2\pi \sqrt{k / M}$
(C) $1 / 2\pi \sqrt{6k / M}$ (D) $1 / 2\pi \sqrt{24k / M}$

42. **(C)** $2(K(L / 2)\theta). L / 2 = (ML^2 / 12)\, \omega^2\theta = \omega^2 = 6K / M$

43. The figure shows the P–V plot of an ideal gas taken through a cycle ABCDA. The part ABC is a semi-circle and CDA is half of an ellipse. Then,



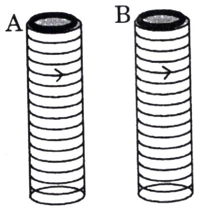
(A) the process during the path $A \rightarrow B$ is isothermal
(B) heat flows out of the gas during the path $B \rightarrow C \rightarrow D$
(C) work done during the path $A \rightarrow B \rightarrow C$ is zero
(D) positive work is done by the gas in the cycle ABCDA

43. **(BD)** In BCD, $\Delta W < O$, $\Delta U < O \Rightarrow \Delta Q, < O$.
In ABC, ΔW = Area of semicircule $\neq$ O.
For $ABCDA$, ΔW = Area within curve $> O$

44. Under the influence of the Coulomb field of charge $+Q$, a charge $-q$ is moving around it in an elliptical orbit. Find out the correct statement(s)
(A) The angular momentum of the charge $-q$ is constant
(B) The linear momentum of the charge $-q$ is constant
(C) The angular velocity of the charge $-q$ is constant
(D) The linear speed of the charge $-q$ is constant

44. **(A)** Elliptical orbit

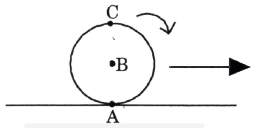
45. Two metallic rings A and B, identical in shape and size but having different resistivities ρ_A and ρ_B, are kept on top of two identical solenoids as shown in the figure. When current I is switched on in both the solenoids in identical manner, the rings A and B jump to heights h_A and h_B, respectively, with $h_A > h_B$. The possible relation(s) between their resistivities and their masses m_A and m_B is (are)



(A) $\rho_A > \rho_B$ and $m_A = m_B$
(B) $\rho_A < \rho_B$ and $m_A = m_B$
(C) $\rho_A > \rho_B$ and $m_A > m_B$
(D) $\rho_A < \rho_B$ and $m_A < m_B$

45. **(BD)** $q_{flow} \propto \rho^{-1}$, $h \propto v^2 \propto (q / m) \propto (1 / m\rho)$.
Since $h_A > h_B$, $m_A \rho_A < m_B \rho_B$.

46. A sphere is rolling without slipping on a fixed horizontal plane surface. In the figure A is the point of contact, B is the centre of the sphere and C is its topmost point Then,



(A) $\vec{V}_C - \vec{V}_A = 2(\vec{V}_B - \vec{V}_C)$
(B) $\vec{V}_C - \vec{V}_B = \vec{V}_B - \vec{V}_A$
(C) $|\vec{V}_C - \vec{V}_A| = 2|\vec{V}_B - \vec{V}_C|$
(D) $|\vec{V}_C - \vec{V}_A| = 4|\vec{V}_B|$

46. **(BC)** $V_A = 0$ & $V_C = 2V_B$.

47. A student performed the experiment to measure the speed of sound in air using resonance air-column method. Two resonances in the air-column ware obtained by lowering the water level. The resonance with the shorter air-column is the first resonance and that with the longer air-column is the second resonance. Then,
(A) the intensity of the sound heard at the first resonance was more than that at the second resonance
(B) the prongs of the tuning fork were kept in a horizontal plane above the resonance tube
(C) the amplitude of vibration of the ends of the prongs is typically around 1 cm
(D) the length of the air-column at the first resonance was somewhat shorter than 1 / 4 the of the wavelength of the sound in air

47. **(D)** Prongs are in vertical plane, amplitude in mm range,
$\lambda + ec = \lambda / 4$

48. This section contains 2 contains 2 questions. Each questions contains statements given in two columns, which have to be matched. The statements in **Column I** are labelled A, B, C and D, while the statements in **Column II** are labelled *p*, *q*, *r*, *s* and *t*. Any given statement in **Column I** can have correct matching with **one or more** statement(s) in **Column II**. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example :

If the correct matches are A – *p*, *s* and *t*; B – *q* and *r* ; C – *p* and *q*; and D – *s* and *t*; then the correct darkening of bubbles will look like the following.

Column II gives certain systems undergoing a process. **Column I** suggests changes in some of the parameters related to the system. Match the statements in **Column I** to the appropriate process(es) from **Column II**.

Column I	Column II
(A) The energy of the system is Increased	(P) System: A capacitor initially uncharged Process: It is connected to a battery
(B) Mechanical energy is provided to the system, which is converted into energy of random motion of its parts	(Q) System: A gas in an adiabatic container fitted with an adiabatic piston Process: The gas is compressed by pushing the piston
(C) Internal energy of the system is converted into its mechanical energy	(R) System: A gas in a rigid container Process: The gas gets cooled due to colder atmosphere surrounding it
(D) Mass of the system is decreased	(S) System: A heavy nucleus initially at rest Process: The nucleus fissions into two fragments of nearly equal masses and some neutrons are emitted
	(T) System: A resistive wire loop Process: The loop is placed in a time varying magnetic field perpendicular to its plane.

48. **(p) → (A)** : elec. energy stored.

(q) → (AB) energy supplied, increasing internal energy

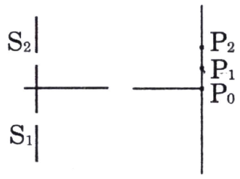
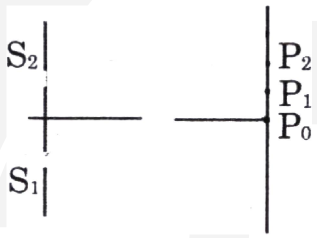
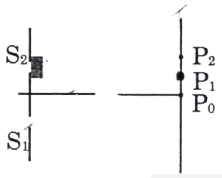
(r) → (none) energy reduces, heat flows out, internal energy drops

(s) → (ACD) Mass to energy coversion

(t) → (A) Current flows leading to heat generation

∴ (A) → (pqst), (B) → (q), (C) → (s), (D) → (s)

49. **Column I** shows four situations of standard Young's double slit arrangement with the screen placed far away from the slits S_1 and S_2. In each of these cases $S_1P_0 = S_2P_0$, $S_1P_1 - S_2P_1 = \lambda / 4$ and $S_1P_2 - S_2P_2 = \lambda/3$, where λ is the wavelength of the light used. In the cases *B*,*C* and *D*, a transparent sheet of refractive index μ and thickness *t* is pasted on slit S_2. The thicknesses of the sheets are different in different cases. The phase difference between the light waves reaching a point *P* on the screen from the two slits is denoted by $\delta(P)$ and the intensity by $I(P)$. Match each situation given in **Column I** with the statement(s) in **Column II** valid for that situation.

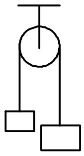
Column I	**Column II**
(A) 	(P) $\delta(P_0) = 0$
(B) $(\mu-1)\, t = \lambda / 4$ 	(Q) $\delta(P_1) = 0$
(C) $(\mu-1)\, t = \lambda / 2$ 	(R) $I(P_1) = 0$
(D) $(\mu-1)\, t = 3\lambda / 4$ 	(S) $I(P_0) > I(P_1)$
	(T) $I(P_2) > I(P_1)$

49. **(A) → (ps), (B) → (q), (C) → (t), (D) → (rst)**

SECTION IV - Integer Answer Type

This section contains 8 questions. The answer to each of the questions is a single digit integer, ranging from 0 to 9. The appropriate bubbles below the respective question numbers in the ORS have to be darkened. For example, if the correct answers to question numbers X,Y,Z and W (say) are 6,0,9 and 2, respectively, then the correct darkening of bubbles will look like the following:

50. A light inextensible string that goes over a smooth fixed pulley as shown in the figure connects two blocks of masses 0.36 kg and 0.72 kg. Taking $g = 10\ ms^{-2}$, find the work done (in joules) by the string on the block of mass 0.36 kg during the first second after the system is released from rest.



50. **8** $a = g / 3$, $T = 4.8$ N, $S = ½ at^2 = 5 / 3$ m. $\Rightarrow W = TS =$ **(in Joule)**

51. Two soap bubbles A and B are kept in a closed chamber where the air is maintained to pressure 8 Nm^{-2}. The radii of bubbles A and B are 2 cm and 4 cm, respectively. surface tension of the ssoap-water used to make bubbles is 0.04 Nm^{-1}. Find the ratio n_B / n_A, where n_A and n_B are the number of moles of air in bubbles A and B, respectively. [Neglect the effect of gravity.]

51. **6** $P_A = P_0 + (4S / r) = 16\ Nm^{-2}$, $P_B = 12\ Nm^{-2}$. $n_B : n_A = P_B V_B : P_A V_A = (3 / 4)$. 8 = **6**

52. A steady current I goes through a wire loop PQR having shape of a right angle triangle with $PQ = 3x$, $PR = 4x$ and $QR = 5x$. If the magnitude of the magnetic field at P due to this loop is $k\left(\frac{\mu_0 I}{48\pi x}\right)$, find the value of k.

52. **7** B only due to QR. $\therefore$ $K\mu_0 I / 48\pi x = (\mu_0 I / 4\pi(2.4x))\ [(3 / 5) + (4 / 5)] = 7\mu_0 I / 48\pi x$ $\Rightarrow K =$ **7**

53. A cylindrical vessel of height 500 mm has an orifice (small hole) at its bottom. The orifice is initially closed and water is filled in it up to height H. Now the top is completely sealed with a cap and the orifice at the bottom is opened. Some water comes out from the orifice and the water level in the vessel becomes steady with height of water column being 200 mm. Find the fall in height (in mm) of water level due to opening of the orifice. [Take atmospheric pressure = $1.0 \times 10^5\ Nm^{-2}$, density of water = 1000 kg m^{-3} and $g = 10\ ms^{-2}$. Neglect any effect of surface tension.]

53. **6** $P_f = P_0 - \rho g H_f = 0.98 \times 10^5$. Since for air, $P_i V_i = P_f V_f$, $1(300 - \Delta H) = 0.98 \times 300 \Rightarrow \Delta H =$ **6 mm**

54. A 20 cm long string, having a mass of 1.0 g, is fixed at both the ends. The tension in the string is 0.5 N. The string is set into vibrations using an external vibrator of frequency 100 Hz. Find the separation (in cm) between the successive nodes on the string.

54. **5** $v = \sqrt{(T / \mu)} = \sqrt{(Tl / m)} = 10\ ms^{-1}$. $\therefore$ $\lambda = v / f = 10$ cm. $\therefore$ $d = \lambda / 2 =$ **5 cm**.

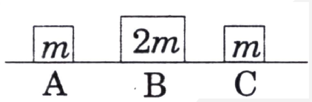
55. A solid sphere of radius R has a charge Q distributed in its volume with a charge dinsity $\rho = Kr^{a}$, where K and a are constants and r is the distance from its centre. If the electric field at $r = R / 2$ is 1/8 times that at $r = R$, find the value of a.

55. **2** $E \propto \int_0^r x^2 x^{\alpha} dx / r^2 \propto r^{\alpha+1}$. Since $E \propto r^3$, α = **2**

56. A metal rod AB of length 10 x has its one end A in ice at 0°C, and the other end B in water at 100°C. If a point P on the rod is maintained at 400°C, then it is found that equal amounts of water and ice evaporate and melt per unit time. The latent heat of evaporation of water is 540 cal g^{-1} and latent heat of melting of ice is 80 cal g^{-1}. If the point P is at a distance of λx from the ice end A, find the value of λ. [Neglect any heat loss to the surrounding.]

56. **9** $KA.400 / \lambda x.80 = KA.300 / ((10 - \lambda)\, x.540) \Rightarrow (10 - \lambda) / \lambda = 1 / 9 \Rightarrow \lambda =$ **9**

57. Three objects A, B and C are kept in a straight line on a frictionless horizontal surface. These have masses m, $2m$ and m, respectively. The object A moves towards B with a speed 9 ms^{-1} and makess an elastic collision with it. There after, B makes completely inelastic collision with C. All motions occur on the same straight line. Find the final speed (in ms^{-1}) of the object C.



57. **4** AB collision : $v_B = 6$ ms^{-1}, BC collision : $V_C = 4$ $ms^{-1} \Rightarrow$ **4**